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Density of Weighted Wavelet Frames.

If $\psi \in L^2(\mathbb{R})$, Λ is a discrete subset of the affine group $\mathbf{A} = \mathbb{R}^+ \times \mathbb{R}$, and $w : \Lambda \rightarrow \mathbb{R}^+$ is a weight function, then the weighted wavelet system generated by ψ , Λ , and w is $\mathcal{W}(\psi, \Lambda, w) = \{w(a, b)^{1/2} a^{-1/2} \psi(\frac{x}{a} - b) : (a, b) \in \Lambda\}$. In this paper we define lower and upper weighted densities $\mathcal{D}_w^-(\Lambda)$ and $\mathcal{D}_w^+(\Lambda)$ of Λ with respect to the geometry of the affine group, and prove that there exist necessary conditions on a weighted wavelet system in order that it possesses frame bounds. We apply these results to oversampled affine systems (which include the classical affine and the quasi-affine systems as special cases), to co-affine wavelet systems, and to systems consisting only of dilations, obtaining some new results relating density to the frame properties of these systems. (Received September 23, 2002)