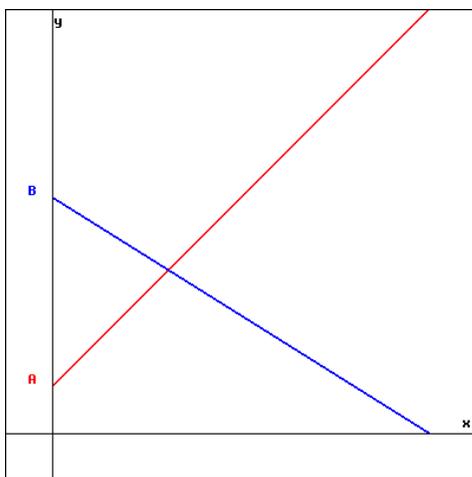


1. (1 pt) UIOWA.pg

Use Cramer's rule to find the point of intersection of the lines in the figure, given that line A, in red, has equation $y = x + 1$ and line B, in blue, has equation $2x + 3y = 10$.

$x = \underline{\hspace{2cm}}$
 $y = \underline{\hspace{2cm}}$



(Click on graph to enlarge)

2. (1 pt) local/Library/UI/ur.la.6.25.pg

Let $A = \begin{bmatrix} -2 & 2 & -1 \\ 1 & 1 & -2 \\ 1 & 2 & 0 \end{bmatrix}$.

Find the following:

(a) $\det(A) = \underline{\hspace{2cm}}$,

(b) the matrix of cofactors $C = \begin{bmatrix} \underline{\hspace{1cm}} & \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \end{bmatrix}$,

Hint: These are the same cofactors you used to find the determinant. Put these cofactors into the above matrix C.

(c) $\text{adj}(A) = \begin{bmatrix} \underline{\hspace{1cm}} & \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \end{bmatrix}$,

Hint: $\text{Adj}(A) = C^T$.

(d) $A^{-1} = \begin{bmatrix} \underline{\hspace{1cm}} & \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \end{bmatrix}$.

Hint: Divide $\text{Adj}(A)$ by the determinant.

3. (1 pt) local/Library/UI/ur.la.6.26.pg

Let $A = \begin{bmatrix} -3e^{3t} & 4e^{2t} \\ -6e^{3t} & -3e^{2t} \end{bmatrix}$.

Find the following:

(a) $\det(A) = \underline{\hspace{2cm}}$,

(b) the matrix of cofactors $C = \begin{bmatrix} \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \end{bmatrix}$,

Hint: These are the same cofactors you used to find the determinant. Put these cofactors into the above matrix C.

(c) $\text{adj}(A) = \begin{bmatrix} \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \end{bmatrix}$,

Hint: $\text{Adj}(A) = C^T$.

(d) $A^{-1} = \begin{bmatrix} \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \end{bmatrix}$.

Hint: Divide $\text{Adj}(A)$ by the determinant.

4. (1 pt) Library/Rochester/setLinearAlgebra4InverseMatrix-ur.la.4.11.pg

If $A = \begin{bmatrix} 2e^{2t} \sin(8t) & -2e^{3t} \cos(8t) \\ -5e^{2t} \cos(8t) & -5e^{3t} \sin(8t) \end{bmatrix}$

then $A^{-1} = \begin{bmatrix} \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \end{bmatrix}$.

5. (1 pt) Library/ASU-topics/set119MatrixAlgebra/p13.pg

Consider the following two systems.

(a)
$$\begin{cases} -6x + 4y = -3 \\ x - y = 3 \end{cases}$$

(b)
$$\begin{cases} -6x + 4y = 3 \\ x - y = 1 \end{cases}$$

(i) Find the inverse of the (common) coefficient matrix of the two systems.

$$A^{-1} = \begin{bmatrix} \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \end{bmatrix}$$

(ii) Find the solutions to the two systems by using the inverse, i.e. by evaluating $A^{-1}B$ where B represents the right hand side (i.e. $B = \begin{bmatrix} -3 \\ 3 \end{bmatrix}$ for system (a) and $B = \begin{bmatrix} 3 \\ 1 \end{bmatrix}$ for system (b)).

Solution to system (a): $x = \underline{\hspace{1cm}}$, $y = \underline{\hspace{1cm}}$

Solution to system (b): $x = \underline{\hspace{1cm}}$, $y = \underline{\hspace{1cm}}$

6. (1 pt) Library/NAU/setLinearAlgebra/systemEquivalent.pg
Determine the following equivalent representations of the following system of equations:

$$\begin{aligned} 7x + 7y &= 0 \\ -2x + 4y &= -18 \end{aligned}$$

a. Find the augmented matrix of the system.

$$\left[\begin{array}{cc|c} _ & _ & _ \\ _ & _ & _ \end{array} \right]$$

b. Find the matrix form of the system.

$$\left[\begin{array}{cc} _ & _ \\ _ & _ \end{array} \right] \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} _ \\ _ \end{bmatrix}$$

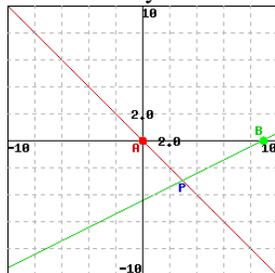
c. Find a matrix that satisfies the following matrix equation.

$$\begin{bmatrix} x \\ y \end{bmatrix} = \left[\begin{array}{cc} _ & _ \\ _ & _ \end{array} \right] \begin{bmatrix} 0 \\ -18 \end{bmatrix}$$

d. Find matrices that satisfy the following matrix equation.

$$x \begin{bmatrix} _ \\ _ \end{bmatrix} + y \begin{bmatrix} _ \\ _ \end{bmatrix} = \begin{bmatrix} _ \\ _ \end{bmatrix}$$

e. The graph below shows the lines determined by the two equations in our system:



Find the coordinates of

$$P = (_, _)$$

Find the coordinates of y-intercept of the red line.

$$A = (0, _)$$

Find the coordinates of x-intercept of the green line.

$$B = (_, 0)$$

7. (1 pt) Library/Rochester/setLinearAlgebra3Matrices/ur_la.3.15.pg

Find a and b such that

$$\begin{bmatrix} 9 \\ 12 \\ 2 \end{bmatrix} = a \begin{bmatrix} 1 \\ 4 \\ -1 \end{bmatrix} + b \begin{bmatrix} 4 \\ -8 \\ 7 \end{bmatrix}.$$

$$a = _$$

$$b = _$$

8. (1 pt) Library/NAU/setLinearAlgebra/HomLinEq.pg

Solve the equation

$$-8x + 6y + 5z = 0$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = s \begin{bmatrix} _ \\ _ \\ _ \end{bmatrix} + t \begin{bmatrix} _ \\ _ \\ _ \end{bmatrix}$$

9. (1 pt) Library/Rochester/setAlgebra34Matrices/scalarmult3.pg

If $A = \begin{bmatrix} -2 & 4 & 4 \\ 2 & -2 & -3 \\ -3 & 2 & 4 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 2 & 0 \\ -4 & -3 & -2 \\ 1 & 2 & 2 \end{bmatrix}$, then

$$3A - 4B = \begin{bmatrix} _ & _ & _ \\ _ & _ & _ \\ _ & _ & _ \end{bmatrix} \text{ and}$$

$$A^T = \begin{bmatrix} _ & _ & _ \\ _ & _ & _ \\ _ & _ & _ \end{bmatrix}.$$

10. (1 pt) Library/Rochester/setLinearAlgebra9Dependence/ur_la.9.3.pg

Let $A = \begin{bmatrix} -14 \\ 26 \\ 30 \\ 2 \end{bmatrix}$, $B = \begin{bmatrix} 0 \\ -1 \\ -3 \\ 5 \end{bmatrix}$, $C = \begin{bmatrix} -4 \\ 7 \\ 7 \\ 3 \end{bmatrix}$, and $D = \begin{bmatrix} 2 \\ -3 \\ -3 \\ -3 \end{bmatrix}$.

1. Determine whether or not the four vectors listed above are linearly independent or linearly dependent.

If they are linearly dependent, determine a non-trivial linear relation - (a non-trivial relation is three numbers which are not all three zero.) Otherwise, if the vectors are linearly independent, enter 0's for the coefficients, since that relationship **always** holds.

$$_ A + _ B + _ C + _ D = 0.$$

11. (1 pt) Library/Rochester/setLinearAlgebra10Bases/ur_la.10.26.pg

Find a basis of the subspace of \mathbb{R}^4 defined by the equation $4x_1 + 5x_2 + 2x_3 - 2x_4 = 0$.

$$\left\{ \begin{bmatrix} _ \\ _ \\ _ \\ _ \end{bmatrix}, \begin{bmatrix} _ \\ _ \\ _ \\ _ \end{bmatrix}, \begin{bmatrix} _ \\ _ \\ _ \\ _ \end{bmatrix} \right\}.$$

12. (1 pt) Library/Rochester/setLinearAlgebra10Bases/ur_la.10.30.pg

Find a basis of the column space of the matrix

$$A = \begin{bmatrix} 2 & 4 & 0 & -3 \\ -2 & 3 & -2 & -1 \\ -6 & -5 & -2 & 5 \end{bmatrix}.$$

$$\left\{ \begin{bmatrix} _ \\ _ \\ _ \end{bmatrix}, \begin{bmatrix} _ \\ _ \\ _ \end{bmatrix} \right\}.$$

13. (1 pt) Library/Rochester/setLinearAlgebra11Eigenvalues/ur_la.11.1.pg

Find the characteristic polynomial of the matrix

$$A = \begin{bmatrix} -4 & -3 \\ 7 & -2 \end{bmatrix}.$$

$$p(x) = \underline{\hspace{2cm}}$$

14. (1 pt) Library/Rochester/setLinearAlgebra11Eigenvalues-ur.la.11.7.pg

The matrix

$$C = \begin{bmatrix} 4 & 0 & -9 \\ -18 & -5 & 18 \\ 0 & 0 & -5 \end{bmatrix}$$

has two distinct eigenvalues, $\lambda_1 < \lambda_2$:
 $\lambda_1 = \underline{\hspace{1cm}}$ has multiplicity $\underline{\hspace{1cm}}$. The dimension of the corresponding eigenspace is $\underline{\hspace{1cm}}$.
 $\lambda_2 = \underline{\hspace{1cm}}$ has multiplicity $\underline{\hspace{1cm}}$. The dimension of the corresponding eigenspace is $\underline{\hspace{1cm}}$.
 Is the matrix C diagonalizable? (enter YES or NO) $\underline{\hspace{1cm}}$

15. (1 pt) Library/Rochester/setLinearAlgebra11Eigenvalues-ur.la.11.18.pg

The matrix $A = \begin{bmatrix} -2 & 0 & 0 \\ 0 & -2 & 0 \\ -2 & 0 & -2 \end{bmatrix}$

has one real eigenvalue. Find this eigenvalue and a basis of the eigenspace.
 eigenvalue = $\underline{\hspace{1cm}}$,

Basis: $\begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix}, \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix}.$

16. (1 pt) Library/Rochester/setLinearAlgebra11Eigenvalues-ur.la.11.24.pg

The matrix $A = \begin{bmatrix} -5 & 0 & 5 & -5 \\ 0 & -5 & -10 & 10 \\ 0 & 0 & 5 & -10 \\ 0 & 0 & 5 & -10 \end{bmatrix}$ has two distinct eigen-

values $\lambda_1 < \lambda_2$. Find the eigenvalues and a basis of each eigenspace.

$\lambda_1 = \underline{\hspace{1cm}}$,
 Basis: $\begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix}, \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix}, \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix},$

$\lambda_2 = \underline{\hspace{1cm}}$,
 Basis: $\begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix}.$

17. (1 pt) Library/Rochester/setLinearAlgebra12Diagonalization-ur.la.12.1.pg

Let $M = \begin{bmatrix} 6 & 2 \\ -1 & 9 \end{bmatrix}.$

Find formulas for the entries of M^n , where n is a positive integer.

$M^n = \begin{bmatrix} \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \end{bmatrix}.$

18. (1 pt) Library/Rochester/setLinearAlgebra17DotProductRn-ur.la.17.2.pg

Let $x = \begin{bmatrix} 5 \\ 5 \\ -1 \\ 5 \end{bmatrix}.$

Find the norm of x and the unit vector in the direction of x .

$\|x\| = \underline{\hspace{1cm}},$
 $u = \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix}.$

19. (1 pt) Library/Rochester/setLinearAlgebra17DotProductRn-ur.la.17.6.pg

Find a vector v perpendicular to the vector $u = \begin{bmatrix} -3 \\ 4 \end{bmatrix}.$

$v = \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix}.$

20. (1 pt) Library/Rochester/setLinearAlgebra17DotProductRn-ur.la.17.7.pg

Find the value of k for which the vectors

$x = \begin{bmatrix} 4 \\ 0 \\ -1 \\ -4 \end{bmatrix}$ and $y = \begin{bmatrix} -3 \\ 1 \\ 3 \\ k \end{bmatrix}$ are orthogonal.
 $k = \underline{\hspace{1cm}}.$

21. (1 pt) Library/Rochester/setLinearAlgebra18OrthogonalBases-ur.la.18.7.pg

Let $A = \begin{bmatrix} -2 & -3 & -4 & 1 \\ 3 & 6 & 6 & -2 \end{bmatrix}.$

Find an orthonormal basis of the kernel of A .

$\begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix}, \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix}.$

22. (1 pt) Library/Rochester/setLinearAlgebra18OrthogonalBases-ur.la.18.11.pg

Let $A = \begin{bmatrix} 1 & 0 & 3 \\ -1 & -3 & 3 \\ 3 & 10 & -11 \end{bmatrix}.$

Find an orthonormal basis of the column space of A .

$\begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix}, \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix}.$

23. (1 pt) Library/TCNJ/TCNJ.CharacteristicPolynomial/problem5.pg

The matrix.

$$A = \begin{bmatrix} 7 & 2 \\ -2 & 3 \end{bmatrix}.$$

has an eigenvalue λ of multiplicity 2 with corresponding eigenvector \vec{v} . Find λ and \vec{v} .

$\lambda = \underline{\hspace{1cm}}$ has an eigenvector $\vec{v} = \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix}$.

24. (1 pt) Library/TCNJ/TCNJ.Diagonalization/problem4.pg

Let: $A = \begin{bmatrix} 11 & -9 \\ 18 & -16 \end{bmatrix}$

Find S, D and S^{-1} such that $A = SDS^{-1}$.

$S = \begin{bmatrix} \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \end{bmatrix}, D = \begin{bmatrix} \underline{\hspace{1cm}} & 0 \\ 0 & \underline{\hspace{1cm}} \end{bmatrix}, S^{-1} = \begin{bmatrix} \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \end{bmatrix}$

25. (1 pt) Library/TCNJ/TCNJ.OrthogonalSets/problem9.pg

Given $v = \begin{bmatrix} -2 \\ 3 \end{bmatrix}$, find the coordinates for v in the subspace W spanned by $u_1 = \begin{bmatrix} 2 \\ 1 \end{bmatrix}$ and $u_2 = \begin{bmatrix} -6 \\ 12 \end{bmatrix}$. Note that u_1 and u_2 are orthogonal.

$v = \underline{\hspace{1cm}} u_1 + \underline{\hspace{1cm}} u_2$

26. (1 pt) Library/TCNJ/TCNJ.VectorEquations/problem3.pg

Let $A = \begin{bmatrix} -3 & -3 & 0 \\ -1 & -3 & 2 \\ -3 & -4 & 1 \end{bmatrix}$ and $b = \begin{bmatrix} -8 \\ -4 \\ -14 \end{bmatrix}$.

1. Determine if b is a linear combination of a_1, a_2 and a_3 , the columns of the matrix A .

If it is a linear combination, determine a non-trivial linear relation - (a non-trivial relation is three numbers which are not all three zero.) Otherwise, enter 0's for the coefficients.

$\underline{\hspace{1cm}} a_1 + \underline{\hspace{1cm}} a_2 + \underline{\hspace{1cm}} a_3 = b$.

27. (1 pt) Library/Utah/College.Algebra/set12.Matrices.and.Determinants

/1050s12p11.pg

The determinant of the matrix

$$A = \begin{bmatrix} 3 & 4 & 0 & 5 \\ 2 & -2 & 0 & 0 \\ 0 & 3 & 0 & 0 \\ 8 & -6 & 1 & -8 \end{bmatrix}$$

is $\underline{\hspace{1cm}}$.

Hint: Find a good row or column and expand by minors.

28. (1 pt) Library/WHFreeman/Holt_linear_algebra/Chaps.1-4

/4.1.77.pg

The null space for the matrix $\begin{bmatrix} 1 & 7 & -2 & 14 & 0 \\ 3 & 0 & 1 & -2 & 3 \\ 6 & 1 & -1 & 0 & 4 \end{bmatrix}$

is $\text{span}\{A, B\}$ where $A = \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix}$ $B = \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix}$

29. (1 pt) Library/WHFreeman/Holt_linear_algebra/Chaps.1-4

/4.2.29a.pg

Find a basis for the null space of the matrix.

$$A = \begin{bmatrix} -3 & -7 \\ 1 & 9 \end{bmatrix}$$

Basis for $\text{null}(A) = \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix}$

30. (1 pt) Library/WHFreeman/Holt_linear_algebra/Chaps.1-4

/4.2.32a.pg

Find a basis for the null space of matrix A .

$$A = \begin{bmatrix} 1 & 0 & -2 & 3 & -1 \\ 0 & 1 & 0 & 2 & 0 \\ 0 & 0 & 0 & 1 & 2 \end{bmatrix}$$

Basis = $\begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix} \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix}$

31. (1 pt) Library/WHFreeman/Holt_linear_algebra/Chaps.1-4

/holt.01.04.028.pg

Find the values of the coefficients a, b and c so that the conditions

$$f(0) = 3, \quad f'(0) = 19, \quad \text{and} \quad f''(0) = -9$$

hold for the function

$$f(x) = ae^x + be^{2x} + ce^{-3x}$$

$a = \underline{\hspace{1cm}}$

$b = \underline{\hspace{1cm}}$

$c = \underline{\hspace{1cm}}$

32. (1 pt) Library/maCalcDB/setAlgebra34Matrices/det.inv.3x3a.pg

Given the matrix

$$\begin{bmatrix} 1 & 0 & -5 \\ 0 & -3 & -2 \\ 4 & 0 & -3 \end{bmatrix}$$

(a) its determinant is: $\underline{\hspace{1cm}}$

(b) does the matrix have an inverse?

33. (1 pt) Library/NAU/setLinearAlgebra/diag3x3.pg

Let $A = \begin{bmatrix} 5 & -8 & -12 \\ 4 & -7 & -6 \\ 2 & -2 & -6 \end{bmatrix}$. Find an invertible matrix P and a diagonal matrix D such that $D = P^{-1}AP$.

$P = \begin{bmatrix} \underline{\hspace{1cm}} & \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \end{bmatrix}$ $D = \begin{bmatrix} \underline{\hspace{1cm}} & \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \end{bmatrix}$

34. (1 pt) local/Library/UI/LinearSystems/diag.pg

Given that the matrix A has eigenvalue $\lambda_1 = 2$ with corresponding eigenvector $\begin{bmatrix} 4 \\ 2 \end{bmatrix}$ and eigenvalue $\lambda_2 = -8$ with corresponding eigenvector $\begin{bmatrix} 0 \\ 1 \end{bmatrix}$, find A .

$$A = \begin{bmatrix} \underline{\hspace{2cm}} & \underline{\hspace{2cm}} \\ \underline{\hspace{2cm}} & \underline{\hspace{2cm}} \end{bmatrix}.$$

35. (1 pt) local/Library/UI/LinearSystems/ur_la_1_19AxB.pg

Solve the system

$$\begin{cases} 4x_1 - 5x_2 + 3x_3 + 2x_4 = 0 \\ -x_1 + x_2 + 2x_3 + 3x_4 = 0 \\ 3x_1 - 4x_2 + 5x_3 + 5x_4 = 0 \\ -3x_1 + 3x_2 + 6x_3 + 9x_4 = 0 \end{cases}$$

$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} = + \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix} s + \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix} t.$$

Solve the system

$$\begin{cases} 4x_1 - 5x_2 + 3x_3 + 2x_4 = 4 \\ -x_1 + x_2 + 2x_3 + 3x_4 = 2 \\ 3x_1 - 4x_2 + 5x_3 + 5x_4 = 6 \\ -3x_1 + 3x_2 + 6x_3 + 9x_4 = 6 \end{cases}$$

$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} = \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix} + \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix} s + \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix} t.$$

If the matrix A corresponds to the coefficient matrix for the above system of equations, then given any vector \vec{b} , the matrix equation $A\vec{x} = \vec{b}$ will always has an infinite number of solutions.

- A. True
- B. False

36. (1 pt) local/Library/UI/LinearSystems/ur_la_1_20vv3.pg

Solve the system

$$\begin{cases} x_1 + 4x_2 - 2x_3 & + 4x_5 + 4x_6 = 0 \\ & -x_4 + 5x_5 + 3x_6 = 0 \\ x_1 + 4x_2 & - 6x_5 + 8x_6 = 0 \end{cases}$$

$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \\ x_6 \end{bmatrix} = \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix} s + \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix} t + \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix} u.$$

Solve the system

$$\begin{cases} x_1 + 4x_2 - 2x_3 & + 4x_5 + 4x_6 = 0 \\ & -x_4 + 5x_5 + 3x_6 = 1 \\ x_1 + 4x_2 & - 6x_5 + 8x_6 = 2 \end{cases}$$

$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \\ x_6 \end{bmatrix} = \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix} + \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix} s + \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix} t + \begin{bmatrix} \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} \end{bmatrix} u.$$

If the matrix A corresponds to the coefficient matrix for the above system of equations, then given any vector \vec{b} , the matrix equation $A\vec{x} = \vec{b}$ will always has an infinite number of solutions.

- A. True
- B. False

37. (1 pt) Library/NAU/setLinearAlgebra/m1.pg

Find the inverse of AB if

$$A^{-1} = \begin{bmatrix} 2 & -5 \\ 3 & 4 \end{bmatrix} \text{ and } B^{-1} = \begin{bmatrix} 4 & 0 \\ 4 & -2 \end{bmatrix}.$$

$$(AB)^{-1} = \begin{bmatrix} \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \end{bmatrix}$$

38. (1 pt) Library/Rochester/setAlgebra34Matrices/cubing_2x2.pg

Given the matrix $A = \begin{bmatrix} 3 & -4 \\ 0 & 2 \end{bmatrix}$, find A^3 .

$$A^3 = \begin{bmatrix} \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \\ \underline{\hspace{1cm}} & \underline{\hspace{1cm}} \end{bmatrix}.$$

39. (1 pt) local/Library/UI/4.1.77.pg

The null space for the matrix $\begin{bmatrix} 1 & 7 & -2 & 14 & 0 \\ 3 & 0 & 1 & -2 & 3 \\ 6 & 1 & -1 & 0 & 4 \end{bmatrix}$

is $\text{span}\{A, B\}$ where $A = \begin{bmatrix} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{bmatrix}$ $B = \begin{bmatrix} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{bmatrix}$

40. (1 pt) local/Library/UI/4.3.3.pg

Find bases for the column space and the null space of matrix A. You should verify that the Rank-Nullity Theorem holds. An equivalent echelon form of matrix A is given to make your work easier.

$$A = \begin{bmatrix} 1 & 0 & -4 & -3 \\ -2 & 1 & 13 & 5 \\ 0 & 1 & 5 & -1 \end{bmatrix} \quad \begin{bmatrix} 1 & 0 & -4 & -3 \\ 0 & 1 & 5 & -1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

Basis for the column space of A = $\begin{bmatrix} \text{---} \\ \text{---} \\ \text{---} \end{bmatrix} \begin{bmatrix} \text{---} \\ \text{---} \\ \text{---} \end{bmatrix}$

Basis for the null space of A = $\begin{bmatrix} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{bmatrix} \begin{bmatrix} \text{---} \\ \text{---} \\ \text{---} \end{bmatrix}$

41. (1 pt) local/Library/UI/6a.pg

The null space for the matrix $\begin{bmatrix} 2 & 0 & 5 \\ -1 & 6 & 2 \\ 4 & 4 & -1 \\ 5 & 1 & 0 \\ 4 & 1 & 1 \end{bmatrix}$

is $\begin{bmatrix} \text{---} \\ \text{---} \\ \text{---} \end{bmatrix}$

42. (1 pt) Library/Rochester/setLinearAlgebra23QuadraticForms-ur.la.23.1.pg

Write the matrix of the quadratic form

$$Q(x) = -4x_1^2 + 2x_2^2 - 6x_3^2 - 5x_1x_2 - 9x_1x_3 - 1x_2x_3.$$

$$A = \begin{bmatrix} \text{---} & \text{---} & \text{---} \\ \text{---} & \text{---} & \text{---} \\ \text{---} & \text{---} & \text{---} \end{bmatrix}.$$

43. (1 pt) Library/Rochester/setLinearAlgebra23QuadraticForms-ur.la.23.4.pg

If $A = \begin{bmatrix} 5 & 8 \\ 8 & -9 \end{bmatrix}$ and $Q(x) = x \cdot Ax$,

Then $Q(e_1) = \text{---}$ and $Q(e_2) = \text{---}$.

44. (1 pt) Library/Rochester/setLinearAlgebra23QuadraticForms-ur.la.23.5.pg

If $A = \begin{bmatrix} 7 & 9 & 7 \\ 9 & 5 & -9 \\ 7 & -9 & -9 \end{bmatrix}$ and $Q(x) = x \cdot Ax$,

Then $Q(x_1, x_2, x_3) = \text{---} x_1^2 + \text{---} x_2^2 + \text{---} x_3^2 + \text{---} x_1x_2 + \text{---} x_1x_3 + \text{---} x_2x_3$.