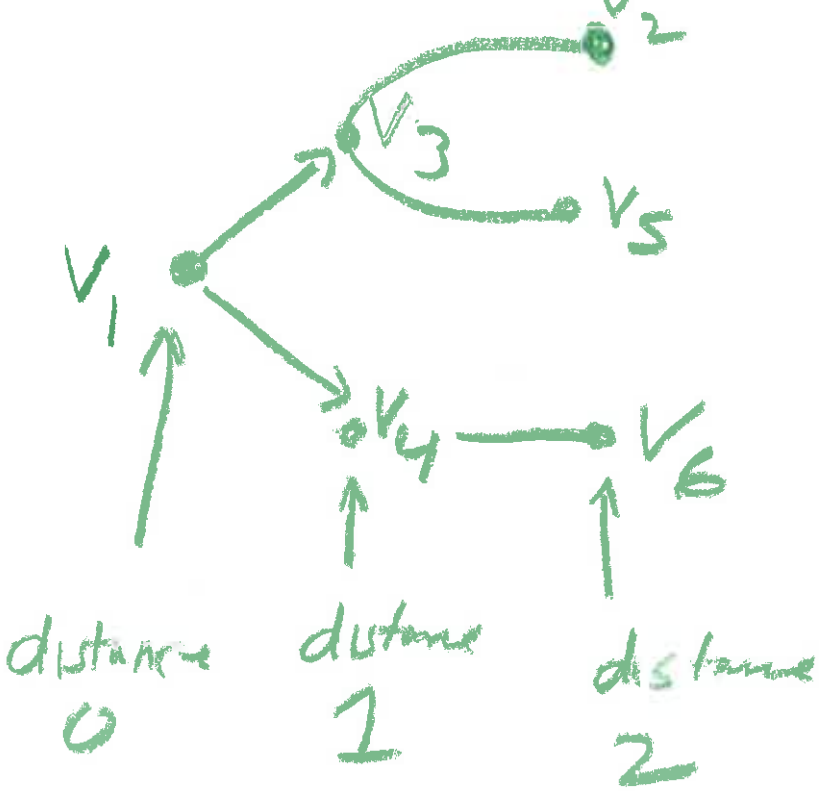
[8] 3.) Suppose a computer program uses the Breadth first search algorithm to determine which vertices are reachable from v_1 where the computer program gives lower indexed vertices priority (i.e., if the program must choose a vertex from a set of vertices, it will choose the one with lowest index). What would be the output if the input is the following adjacency matrix for a directed graph? **You do <u>not</u> need to show work.**

$$\begin{pmatrix} 0 & 0 & 2 & 2 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 1 \\ 1 & 1 & 0 & 0 & 5 & 0 \\ 1 & 0 & 0 & 0 & 0 & 3 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

The vertices reachable from v_1 are

$$v_1, v_2, v_3, v_4, v_5, v_6$$

Draw the tree created by the Breadth first search algorithm. Note this problem is related to problem 4 (same weighted adjacency matrix), but the ouput is not the same.



[5] 4a.) Define: A vertex w is reachable from a vertex v if

$\exists$ a path from v to w

[15] 4b.) Suppose a computer program uses Dijkstra's algorithm to find a shortest path from the vertex v_1 to the vertex v_6 where the computer program gives lower indexed vertices priority (i.e., if the program must choose a vertex from a set of vertices, it will choose the one with lowest index). What would be the output if the input is the following adjacency matrix for a directed graph?

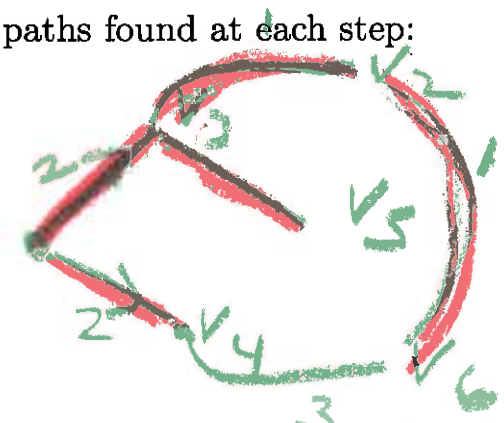
$$\begin{pmatrix} 0 & 0 & 2 & 2 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 1 \\ 1 & 1 & 0 & 0 & 5 & 0 \\ 1 & 0 & 0 & 0 & 0 & 3 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Show your work:

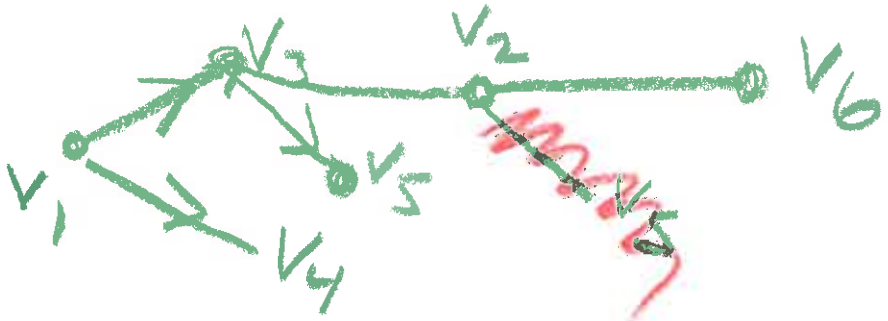
$S = \{v_1, v_3, v_4, v_2, v_6, v_5\}$

The table showing length of shortest paths found at each step:

v_1	v_2	v_3	v_4	v_5	v_6
0	∞	∞	∞	∞	∞
	∞	2	2	∞	∞
	3		2	7	∞
	3			7	5
				7	4
				7	



Note that every vertex is reachable from the vertex v_1. Thus Dikstra's algorithm outputs a spanning tree when starting at v_1. Draw this spanning tree:



What is a shortest path from the vertex v_1 to the vertex v_6?

$$v_1, <\overrightarrow{v_1, v_3}>, v_3, <\overrightarrow{v_3, v_2}>, v_2, <\overrightarrow{v_2, v_6}>, v_6$$