

1.1:

Equilibrium Solution

Graphed slope field of  $\frac{dv}{dt} = f(t, v)$

\*\*\* can use slope field to determine behavior of  $v$  including as  $t \rightarrow \infty$ .

1.2:

Solved  $\frac{dy}{dt} = a(y - \frac{b}{a})$

Solution:  $y = \frac{b}{a} + ce^{at}$

Initial Value Problem:  $y(0) = y_0$

$t = 0, y = y_0$ , then  $c = y_0 - \frac{b}{a}$

1.3:

ODE vs PDE

order of differential eq'n: order of highest derivative

example of order  $n$ :  $y^{(n)} = f(t, y, \dots, y^{(n-1)})$

## Linear vs Non-linear

linear:  $a_0(t)y^{(n)} + \dots + a_n(t)y = g(t)$

## Existence and Uniqueness of Solutions

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CH 2: Solve  $\frac{dy}{dt} = f(t, y)$

2.1: First order linear eqn:  $\frac{dy}{dt} + p(t)y = g(t)$

Ex 1:  $y' = -ay + b$

Ex 2:  $y' + 3t^2y = t^2, y(0) = 0$

Note: could use section 2.2 method, separation of variables to solve ex 1 and 2.

Ex 3:  $t^2y' + 2ty = t\sin(t)$