

To solve linear DE $ay'' + by' + cy = g_1 + g_2 + g_3$

Step 1: Solve homogeneous version: $ay'' + by' + cy = 0$ implies

$$ar^2 + br + c = 0 \text{ implies } \dots \quad y = c_1\phi_1 + c_2\phi_2.$$

Step 2a: Find one non-homogeneous solution, $y = f_1$, to $ay'' + by' + cy = g_1$

Step 2b: Find one non-homogeneous solution, $y = f_2$, to $ay'' + by' + cy = g_2$

Step 2c: Find one non-homogeneous solution, $y = f_3$, to $ay'' + by' + cy = g_3$

Step 3: Combine all solutions to create the general solution to the non-homogeneous DE:

$$y = c_1\phi_1 + c_2\phi_2 + f_1 + f_2 + f_3$$

Last step: If IVP, plug in initial values to find the constants c_1 and c_2 .

Guess a possible non-homog soln for the following DEs:

Note homogeneous solution to $y'' + 2y' + y = 0$ is

$$y = c_1e^{-t} + c_2te^{-t} \text{ since } r^2 + 2r + 1 = (r + 1)(r + 1) = 0$$

1.) $y'' + 2y' + y = 4e^{2t}$

Guess: _____

2.) $y'' + 2y' + y = 4e^t$

Guess: _____

3.) $y'' + 2y' + y = 4e^{-t}$

Guess: _____

4.) $y'' + 2y' + y = t$

Guess: _____

5.) $y'' + 2y' + y = t + 1$

Guess: _____

6.) $y'' + 2y' + y = 4\sin(2t)$

Guess: _____

7.) $y'' + 2y' + y = 4\sin(2t) + 5\cos(2t)$

Guess: _____

8.) $y'' + 2y' + y = 4\sin(2t) + 5\cos(3t)$

Guess for step 2a: _____

Guess for step 2b: _____

9.) $y'' + 2y' + y = 4\sin(2t) + t + 1$

Guess for step 2a: _____

Guess for step 2b: _____

10.) $y'' + 2y' + y = 4t\sin(2t)$

Guess: _____

11.) $y'' + y = 4\sin(2t)$

Guess: _____

12.) $y'' + y = 4\sin(t)$

Guess: _____