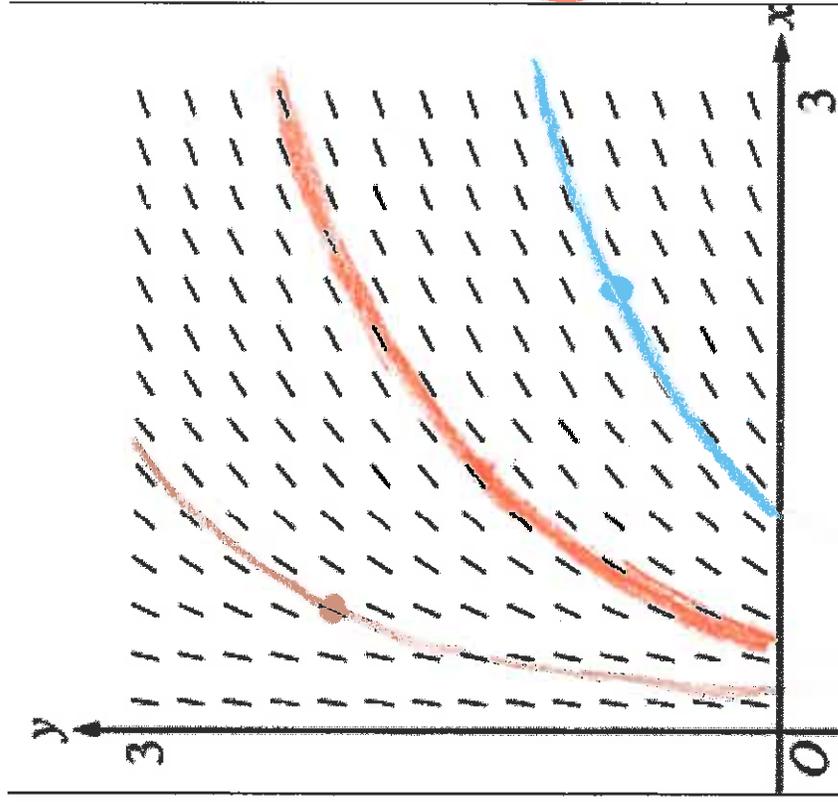


From the May 2008 AP Calculus Course Description:
15.

From: http://apcentral.collegeboard.com/apc/public/repository/ap08_calculus_slopefields_worksheet.pdf



No ATTENDANCE QUIZ TODAY

$$y' = \frac{1}{x}$$

~~(A) $y = x^2$~~ ~~(B) $y = e^x$~~ ~~(C) $y = e^{-x}$~~ ~~(D) $y = \cos x$~~ (E) $y = \ln x$

- (A) $y = x^2$ (B) $y = e^x$ (C) $y = e^{-x}$ (D) $y = \cos x$ (E) $y = \ln x$

The slope field from a certain differential equation is shown above. Which of the following could be a specific solution to that differential equation?

- (A) $y = x^2$ (B) $y = e^x$ (C) $y = e^{-x}$ (D) $y = \cos x$ (E) $y = \ln x$

2.3: Modeling with differential equations.

Suppose salty water enters and leaves a tank at a rate of 2 liters/minute.

Suppose also that the salt concentration of the water entering the tank varies with respect to time according to $Q(t) \cdot t \sin(t^2)$ g/liters where $Q(t)$ = amount of salt in tank in grams. (Note: this is not realistic).

If the tank contains 4 liters of water and initially contains 5g of salt, find a formula for the amount of salt in the tank after t minutes.

Let $Q(t)$ = amount of salt in tank in grams.

Note $Q(0) = 5$ g

$$\begin{aligned} \text{rate in} &= (2 \text{ liters/min})(Q(t) \cdot t \sin(t^2) \text{ g/liters}) \\ &= 2Q t \sin(t^2) \text{ g/min} \end{aligned}$$

$$\text{rate out} = (2 \text{ liters/min})\left(\frac{Q(t) \text{ g}}{4 \text{ liters}}\right) = \frac{Q}{2} \text{ g/min}$$

$$\frac{dQ}{dt} = \text{rate in} - \text{rate out} = 2Q t \sin(t^2) - \frac{Q}{2}$$

$$\frac{dQ}{dt} = Q(2t \sin(t^2) - \frac{1}{2})$$

This is a first order linear ODE. It is also a separable ODE. Thus can use either 2.1 or 2.2 methods.

$Q(0) = 5$
initial condition