## Mathematics 150 Assignment 10 - F. Goodman <br> December, 2007

Use generating function models to solve the following exercises:

1. Find the number of ways to select 25 balls from a pile of red, white and blue balls if:
(a) The selection has at least two red and at least two white balls.
(b) The selection has at most 3 red balls.
(c) The selection has an even number of blue balls.
2. How many ways can we order lunch for the 12 people in our class if their are 5 types of sandwiches available, but at most 4 sandwiches of any one type are available?
3. How many ways are there to distribute 1 dollar (in pennies) to 10 children and one adult, if the adult receives either 5 cents or 10 cents and each child receives at most 15 cents?
4. A coin is flipped 25 times, and exactly 8 tails occur. In how many ways can this be done (i.e. how many sequence of 25 H's and T's with 8 T's). In how many ways can this be done so that there are no runs of 6 or more heads?
5. A probability generating function $p_{X}(t)$ for a discrete random variable $X$ is a power series $\sum_{r} p_{r} t^{r}$, where $p_{r}$ is the probability that the random variable takes the value $r$.
(a) Let $X$ be the number of heads that occur when a fair coin is flipped $n$ times. Find $p_{X}(t)$.
(b) Let $X$ be the number of times a fair coin is flipped until the 5 th head occurs. Find $p_{X}(t)$.
